# Studies on Thermal Degradation of Synthetic Polymers. XV. Estimation of the Product Yield on the Basis of Intensity Function for Thermal Gasification of Isotactic and Atactic Polypropylenes

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#### Synopsis

The kinetic equation for the pyrolysis gasification reaction of isotactic and atactic polypropylenes has been established. The difference in tacticity of the samples does not much affect the kinetic parameters. The exponent *a* of the intensity function  $I_F = T\theta^a$  (K-sec<sup>*a*</sup>), concerning the severity of decomposition conditions, has been approximated as 0.039 (isotactic) and 0.040 (atactic), respectively from the kinetic parameters in this experiment. The calculated values of the product yield from Arrhenius equations,  $k = 2.0 \times 10^{10} \exp(-40.9 \times 10^3/RI_F)$  (isotactic) and  $k = 1.2 \times 10^{10} \exp(-41.4 \times 10^3/RI_F)$  (atactic), for the  $I_F$  standard agree with the experimental values.

#### INTRODUCTION

From the point of view of energy diversification and chemical resources, attention has been directed not only to coal and heavy oils of the petroleum group, but also to plastic waste matter and recovery of resources by pyrolysis. The most suitable control method of recovery by pyrolysis requires development of a way for estimating product yield corresponding to the decomposition conditions. The prediction of product yield should be made on the basis of kinetics, i.e., by the analysis of the equations of material balance maintained through various elementary reactions which occur by free radical mechanisms. However, the analysis of the elementary reactions, even in the thermal decomposition of petroleum hydrocarbons,<sup>1</sup> becomes very difficult with an increase in the number of carbon atoms in a sample, and it is impossible to analyze the elementary reactions in the case of polymers. The authors therefore have directed their attention to the parameter that expresses the degree of severity of the decomposition conditions, i.e., the intensity function  $(I_F = T\theta^a)$ , and has good correlation with the product yield. From experience,  $0.06^2$  is used as the value for the exponent a, and this value is also applied for the pyrolysis of crude petroleum.<sup>3</sup> The authors<sup>4-7</sup> introduced the concept of  $I_F$  for polymers; and in cases where property values differ completely from naphtha, crude petroleum, etc., an experimental induction method for the value of a was established. It was demonstrated that  $I_F$  has a good correlation with the product yield. Moreover, the value of a for polymers differs from that for petroleum hydrocarbons, and it was suggested that the value of a is dependent on the molecular structure of the sample and that it is correlated with the kinetic parameter (activation energy).<sup>4</sup>  $I_F$  is useful as a means for estimating product yield, and it is clear that the value of a depends considerably on the pyrolysis reaction according to the type of material.

In order to use the concept of  $I_F$  for the pyrolysis reaction with a wide range of hydrocarbons, it is necessary to elucidate the value of a theoretically. Davis and Farrell<sup>2</sup> have recently indicated a definition of  $I_F$  ( $I_F$  corresponds to the temperature required to obtain an optical conversion ratio x in a residence time of 1 sec) and established an  $I_F$  standard kinetic equation using a = 0.062. It is noteworthy as a first attempt that elucidation of the relation between  $I_F$  and kinetics was made from the definition of  $I_F$ . Recently, the authors<sup>8</sup> have established a kinetic equation for the pyrolysis gasification reaction of polyethylene-low polymers, theoretically clarified  $I_F$ , which is conventionally considered an important parameter, from a kinetic point of view, and clarified the dependence of the kinetic parameters on the value of the exponent a of  $I_F$ . Moreover, the authors have developed a useful means for estimating the product yield from  $I_F$  on the basis of the kinetic parameter, which quantitatively reflects the pyrolysis reactions.

In this study,  $I_F$  is shown to be applicable to the thermal gasification of isotactic and atactic polypropylenes.

## Calculation of Product Yield on the Basis of the Theoretical Relation between I<sub>F</sub> and Kinetics

The relation between the value for the exponent a on  $I_F$  and the kinetic parameters have been described in a previous report.<sup>8</sup>

The intensity function equation, first-order reaction velocity equation, and Arrhenius equation are as follows:

$$I_F = T\theta^a \tag{1}$$

$$\frac{dx}{d\theta} = k(1-x) \tag{2}$$

or

$$k = \ln (1 - x)^{-1/\theta}$$
  

$$k = A \exp(-E/RT)$$
(3)

where  $I_F$  is the intensity function (K-sec<sup>*a*</sup>); *T*, the reaction temperature (K),  $\theta$  = the residence time (sec); *a*, the constant; *x*, the conversion ratio (gasification ratio); *k*, the reaction velocity constant (sec<sup>-1</sup>); *A*, the frequency factor (sec<sup>-1</sup>); *E*, the activation energy (cal/mole); and *R*, the gas constant (cal/mole K). Equations (4) and (5) are obtained when the above definition of  $I_F$  is introduced into eqs. (2) and (3):

$$k_{IF} = \ln (1 - x)^{-1} \tag{4}$$

$$k_{IF} = A_{IF} \exp(-E_{IF}/RI_F) \tag{5}$$

with  $k_{IF} = I_F$  standard reaction velocity constant (sec<sup>-1</sup>),  $A_{IF} = I_F$  standard frequency factor (sec<sup>-1</sup>), and  $E_{IF} = I_F$  standard activation energy (cal/mole). Accordingly, the value of *a* can be expressed by the following equation:

$$a = \frac{-\ln\left(1 - \ln\theta \cdot RT/E\right)}{\ln\theta} \tag{6}$$

If  $A = A_{I_F}$  and  $E = E_{I_F}$  hold in the variable range of  $\theta \neq 1$ , eq. (6) becomes a general formula.

Comparison of eqs. (7) and (8) permits evaluation of the value of a obtained from eq. (6) by kinetic consideration:

$$\theta_2 = \theta_1 \left(\frac{T_1}{T_2}\right)^{1/a} \tag{7}$$

$$\theta_2 = \theta_1 \exp\left[\left(\frac{1}{T_2} - \frac{1}{T_1}\right)\frac{E}{R}\right]$$
(8)

Therefore, computation of the product yield on the basis of  $I_F$  is carried out by the following equation:

$$x = 1 - \frac{1}{\exp[A \exp(-E/RI_F)]} \tag{9}$$

#### **EXPERIMENTAL**

**Sample.** In this experiment, the commercial isotactic and atactic forms of polypropylene were used without further purification. The molecular weights and the tacticity are given in Table I.

**Apparatus and Procedure.** The apparatus used and the procedure for this experiment have been described in a previous report<sup>8</sup> in detail. The samples were melted according to the reaction conditions at 200°C (isotactic) and 85°C (atactic) by constant electric heating.

**Analysis.** The gaseous product was analyzed by a Shimadzu 4B-PT gas chromatograph. The conditions for the analysis of each object have already been reported.<sup>5</sup> The average molecular weight was determined by gel permeation chromatography using a Toyo Soda HLC-811 high-speed liquid chromatograph. The calibration line was produced by standard polystyrene, and 26.4 (ref. 9) was used as the Q factor. The tacticity was obtained by <sup>13</sup>C NMR spectrometry using a Jeol JNM-FX 100 spectrometer.

**Definition of Terms.** Definition of the residence time, the effective reactor volume, and the gasification ratio, etc. have been described in a previous report.<sup>8</sup>

Characteristization of Samples Used							
			Microtacticity				
Sample	$\overline{M}_n \times 10^{-3}$	$\overline{M}_w \times 10^{-4}$	mm	mr	rr		
Isotactic	54.8	36.4	0.92	0.06	0.02		
Atactic	3.20	1.68	0.46	0.28	0.26		

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1269

## **RESULTS AND DISCUSSION**

## **Effect of Reaction Conditions on Gasification**

The IR spectra for liquid products obtained under conditions of differing gasification ratios are shown in Figure 1. Up to a gasification ratio of approximately 0.5, the main constituent in liquid products was formed by such aliphatic olefins as the terminal vinylidene (1780, 888 cm<sup>-1</sup>) type. With a gasification ratio of 0.5 or more, aromatics (1600, 1500 cm<sup>-1</sup>, etc.) could be observed, and their absorption appeared stronger with an increase in the gasification ratio. Figure 2 shows the composition of gaseous products for the gasification ratio. With



Fig. 1. IR spectra of pyrolysis products from isotactic polypropylene.



Fig. 2. Composition of gaseous products corresponding to the gasification ratio.

a gasification ratio near 0.5, the product gas composition showed a constant ratio. With a gasification ratio of 0.5 or more, the composition showed a remarkable change. It is believed that secondary reactions such as the redecomposition of olefins take place, and these olefins are the initial products of the gasification reaction and the formation of aromatics by condensation, etc. The IR spectra characterization and the composition for atactic forms are similar to those for isotactic forms mentioned above.

For the gasification reaction of polypropylenes, and polyethylene-low polymers<sup>8</sup>, two reaction ranges can be observed: the first-stage reaction occurs within a gasification ratio range of up to 0.5, where the gas composition is formed at fixed ratio; and the second-stage reaction occurs within a gasification ratio range of 0.5 or higher, where the secondary reactions of the product gas are brought about. For the first-stage reaction range, the following quantitative chemical equation is obtained:

$$[polymer] \rightarrow [depolymerized polymer] \rightarrow a CH_4 + b C_2H_4 + c C_2H_6 + d C_3H_6 + e C_3H_8 + f C_4H_8 + g H_2 \quad (10)$$

The coefficients of each component are expressed by mole fraction in the gaseous products. The coefficients are given in Table II.

### Kinetics of Gasification and $I_F$

As shown in eqs. (2) and (10), these experiments on polypropylenes, as well as polyethylene-low polymers,<sup>8</sup> are governed by overall first-order reaction kinetics in regard to the depolymerized polymer weight fraction for the complicated gasification reaction, and the gasification velocity is analyzed.

A linear relation is established for the plot of  $-\ln(1-x)$  vs.  $\theta$  in the range of short residence times. For the long residence times, the above-mentioned secondary reaction of olefins occurs and linearity is lost. The various reaction velocity constants of the first-stage reaction range are obtained from the slope of the straight line and are shown in the Arrhenius equation (Fig. 3) as

$$k = 2.0 \times 10^{10} \exp\left(\frac{-40.9 \times 10^3}{RT}\right) \text{(isotactic)} \tag{11}$$

$$k = 1.2 \times 10^{10} \exp\left(\frac{-41.4 \times 10^3}{RT}\right)$$
 (atactic) (12)

	Coefficient <sup>a</sup>	Sample		
Component		Isotactic	Atactic	
CH <sub>4</sub>	a	0.13	0.13	
$C_2H_4$	Ь	0.19	0.17	
$C_2H_6$	С	0.07	0.07	
$C_3H_6$	d	0.42	0.40	
$C_3H_8$	е	0.02	0.02	
$C_4H_8$	f	0.15	0.14	
$H_2$	g	0.02	0.07	

TABLE II Coefficients of Each Component in Eq. (10)

<sup>a</sup> Mole fraction in the gaseous products.



As shown in Table II and in eqs. (11) and (12), the difference in the tacticity of both samples dose not have much effect on the gasification reactions.

Comparison of eqs. (3) and (5) clearly shows good coincidence of  $A = A_{I_F}$  as well as  $E = E_{I_F}$  (ref. 8). Accordingly, it becomes clear that the value of a can be calculated by the kinetic parameters shown in eq. (6). Figure 4 shows the change range corresponding to the experimental conditions for the value of a in eq. (6). Since the change range for the value of a is determined by the residence time, reaction temperature, activation energy, frequency factor, and the conversion ratio (gasification ratio), an approximated value can be obtained within the experimental conditions wherein the kinetic parameters are definite. Since the value of a obtained from the kinetic parameters in this experiment changes in the shaded part of the figure, a is approximated as 0.039 (isotactic) and 0.040 (atactic).

Evaluation of the value of a obtained from the kinetic parameters is determined by a comparison of eq. (7) with eq. (8). Figure 5 shows the change of  $T_2$ 



Fig. 4. Change range for the value of a in eq. (6).



Fig. 5. Comparison of eqs. (7) and (8).

and  $\theta_2$  for given values of  $T_1$  and  $\theta_1$ . Equation (7), using a = 0.039 (isotactic) as obtained from the kinetic parameters for this experiment, and eq. (8), using  $E = 40.9 \times 10^3$  cal/mole (isotactic), show good coincidence. This figure also shows considerable dependence of the value of a on the activation energy.



Fig. 6. Comparison of the experimental values with the calculated values for the various product yields on  $I_{F}$ : (**\square**) X; (**\square**)  $C_{1}H_{4}$ ; (**\square**)  $C_{2}H_{4}$ ; (**\square**)  $C_{3}H_{6}$ .

Figure 6 shows a comparison of the experimental values with the calculated values for various product yields based on  $I_F$ , as shown in eq. (9). The calculated and experimental values show good coincidence up to a gasification ratio near 0.5 (first-stage reaction range)

As mentioned above, it has been demonstrated that the theory of  $I_F$  for estimating product yield is also applicable to the thermal gasification of polypropylene.

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